## Math Journal: Football \& Parabolas

| First <br> Score: | First attempt due: | Final |
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During a football game, a team has four plays, or downs to advance the football at least ten yards. After a first down is gained, the team has another four downs to gain ten or more yards.

If a team does not move the football ten yards or more after three downs, then the team has the option of punting the football. By punting the football, the offensive team gives possession of the ball to the other team. Punting is the logical choice when the offensive team (1) is a long way from making a first down, (2) is out of field goal range, and (3) is not in a critical situation.

The punter receives the football about 10 to 12 yards behind the current position on the field. He drops the ball from his hands to kick it, so the ball is in air above the ground when the kick is made. The punter's job is to kick the football as far down the field as possible without the ball going into the end zone.

A punter kicked the football for a distance of 42.1 yards. The path of travel for the football can be modeled by the function $f(x)=-0.208(x-21)^{2}+93$ where $x$ is the distance (in yards) and $y$ is the height (in feet) the football is kicked.

1. Does the graph have a maximum y-value or a minimum $y$-value? Explain how you can tell from looking at the equation that models the path of the football.
2. Find the coordinates of the vertex. What is the maximum height of the football? Label your answer with units.
3. Find the y-intercept. Show work and round to three decimal places. Explain, in the context of the problem, why the $y$-intercept is not $(0,0)$. (Hint: Re-read the $3{ }^{\text {rd }}$ paragraph.)
4. What is the approximate height of the football when it has traveled 8 yards? Show work and round to three decimal places. Based on this result, what are the coordinates of a point on the graph?
5. What is the coordinate of the $x$-intercept? Explain how you know. (Hint: Re-read the last paragraph.)
6. Neatly graph the quadratic function. Label the coordinates on the graph for the vertex, the $y$ intercept, the x-intercept, and at least three more points.


On fourth down, a team is just out of field goal range. The punter is called in. To avoid kicking the ball into the end zone, he needs to kick the ball high and short to get it as close to the opposing end zone as possible without going in. If he gets it to the 1 yard line, the opposing team has to run it almost the full length of the football field to score. His
punt can be modeled by the function $f(x)=-0.461(x-15)^{2}+105$ where $x$ is the distance (in yards) and y is the height (in feet) the football is kicked.
7. Neatly graph the function. Label the coordinates on the graph for the vertex, the y-intercept, and at least three more points.

8. Approximate the coordinate of the $x$-intercept on the graph above. If the kicker was at the 40 -yard line when he punted as shown below, did the ball reach the end zone when it landed? If not, where did it land? Explain.


